

Current Status of Modeling Wolf-Rayet Atmospheres

D. John Hillier

University of Pittsburgh

General Thoughts

Key assumptions

Beals model (hot core surrounded by dense out-flowing wind)

Spherical (but some exceptions)

Key requirements

Atomic data

Line and continuum cross-sections

Collision rates

Charge exchange

Do details matter?

Accurate wavelengths?

Completeness of opacities?

All species?

Clumping

Volume filling factor approach

Macro-clumping

Shell models

Fragmented winds (Dessart and Owocki)

Inhomogenous models are intrinsically 3D, but may be globally 1D.

General Thoughts

Hydrodynamics

- Smooth

- Clumped

- Time dependent

 - Do “static” solutions exist?

Stellar issues

- Pulsations

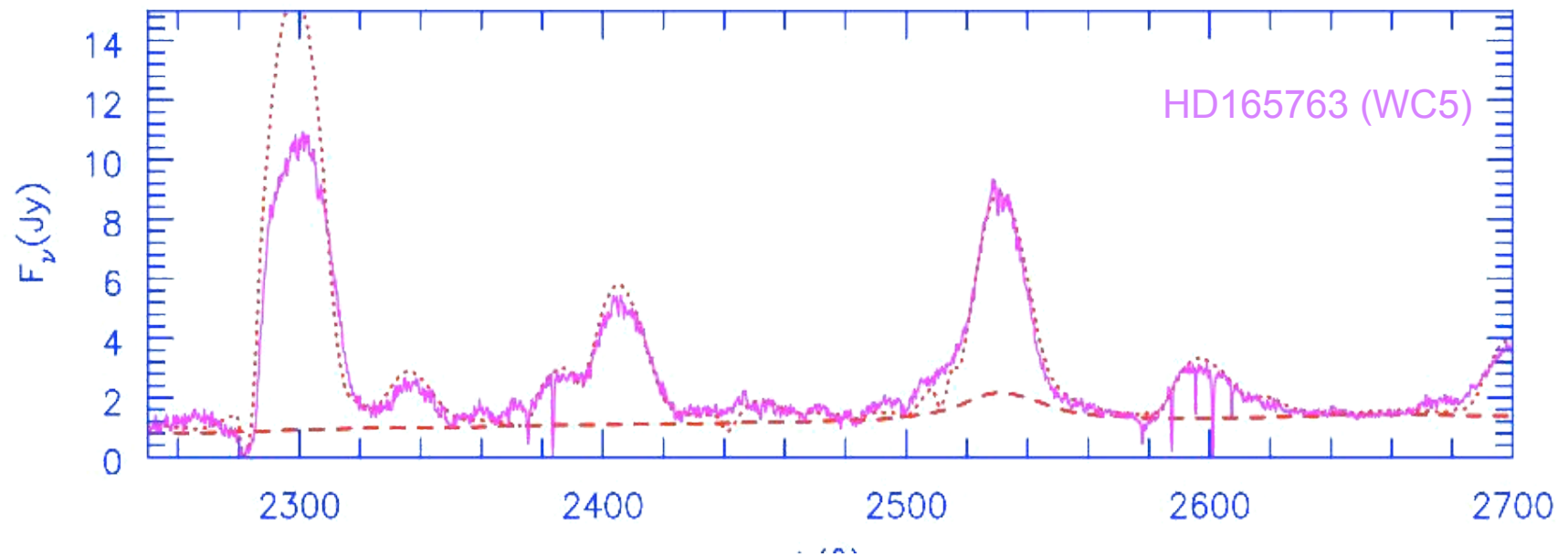
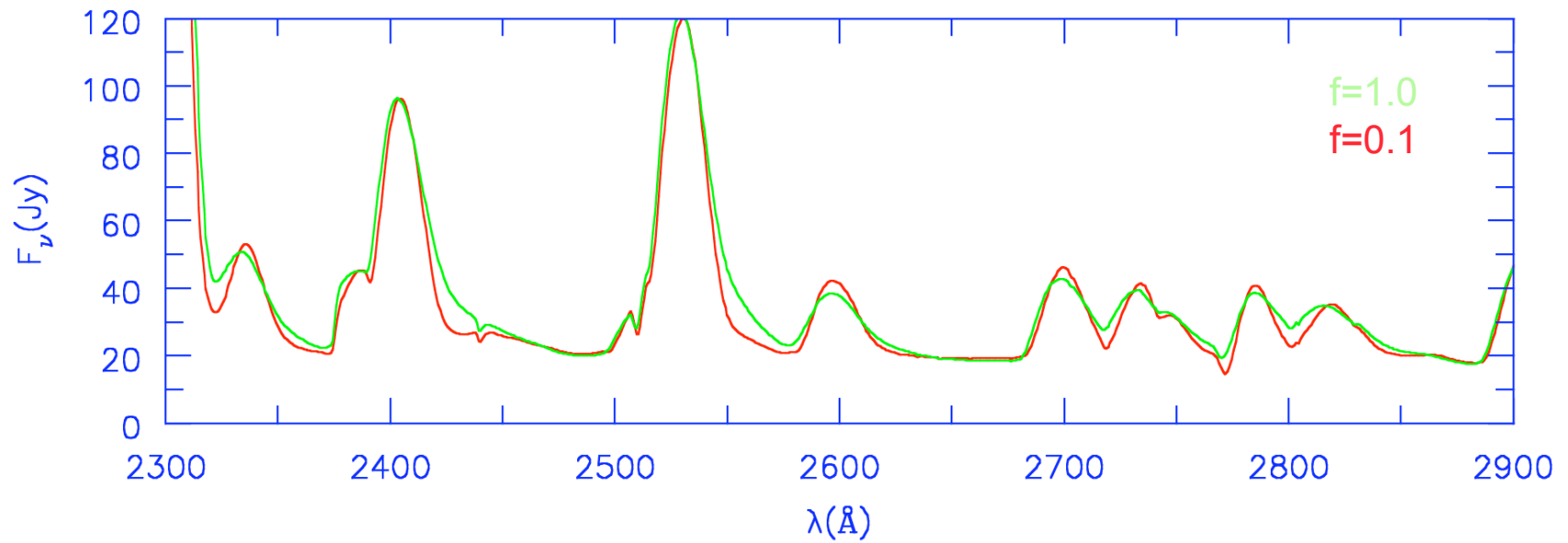
- Instabilities near Eddington limit

Other issues

- Distances

- Reddening ($E(B-V)$ and R)

Hillier & Miller (ApJ, 1999)



Reliability

Abundances

Accurate H/He

CNO (50%)

Fe (factor of 2?)

Abundances not strong function of model.

V_{inf}

10% (turbulence; meaning?)

Mass-loss rates

$\dot{M}_{\text{dot}}/\sqrt{f}$ -- some dependence on β

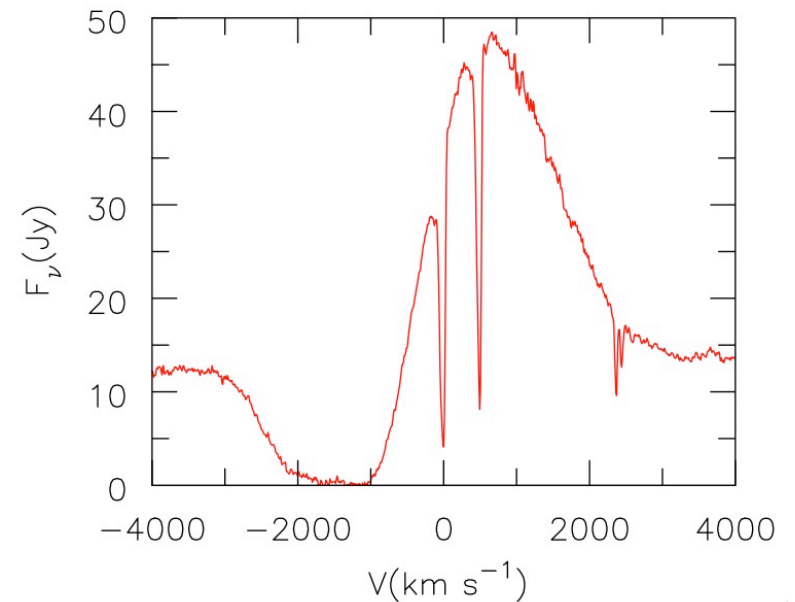
f (factor of 2)

$f(r)$?

Luminosities

50%?

Factor of 2 (or more) increase in L when line blanketing included?



Reliability

Radii

Wind dependent.

Biased by assumptions.

Hydrodynamics: values more consistent with evolution?

Thick winds \Rightarrow difficult to constrain observationally.

Effective temperatures

As for radii

$V(r)$

Thick winds \Rightarrow difficult to constrain observationally.

Hydrodynamics?

Stellar masses

Binaries.

Mass loss rates (sensitive to Γ)

Mass loss Rates from 1st Principals

Fe Opacity bumps (OPAL, Opacity Project)

Nugis & Lamers (2002, A&A, 389 162)

Graefener & Hamann (2005, A&A, 432, 633)

Graefener & Hamann (2008, A&A, 482, 945)

- * Optically thick stellar winds
- * Critical point is sonic point
- * Opacity increases through critical point

Require $T(\text{sonic})$

160,000 K (hot bump)

40,000 to 70,000 K (cool bump)

- * No guarantee that \dot{M} set by critical point can be driven to infinity.
- * Multiple critical points?

Momentum Equation

$$v \frac{dv}{dr} = -\frac{GM(1-\Gamma)}{r^2} - \frac{1}{\rho} \frac{dP}{dr} + g(rad)$$

where

$$g(rad) = \frac{4\pi}{\rho c} \int_0^\infty (\chi_v - \chi_{es}) H_v dv$$

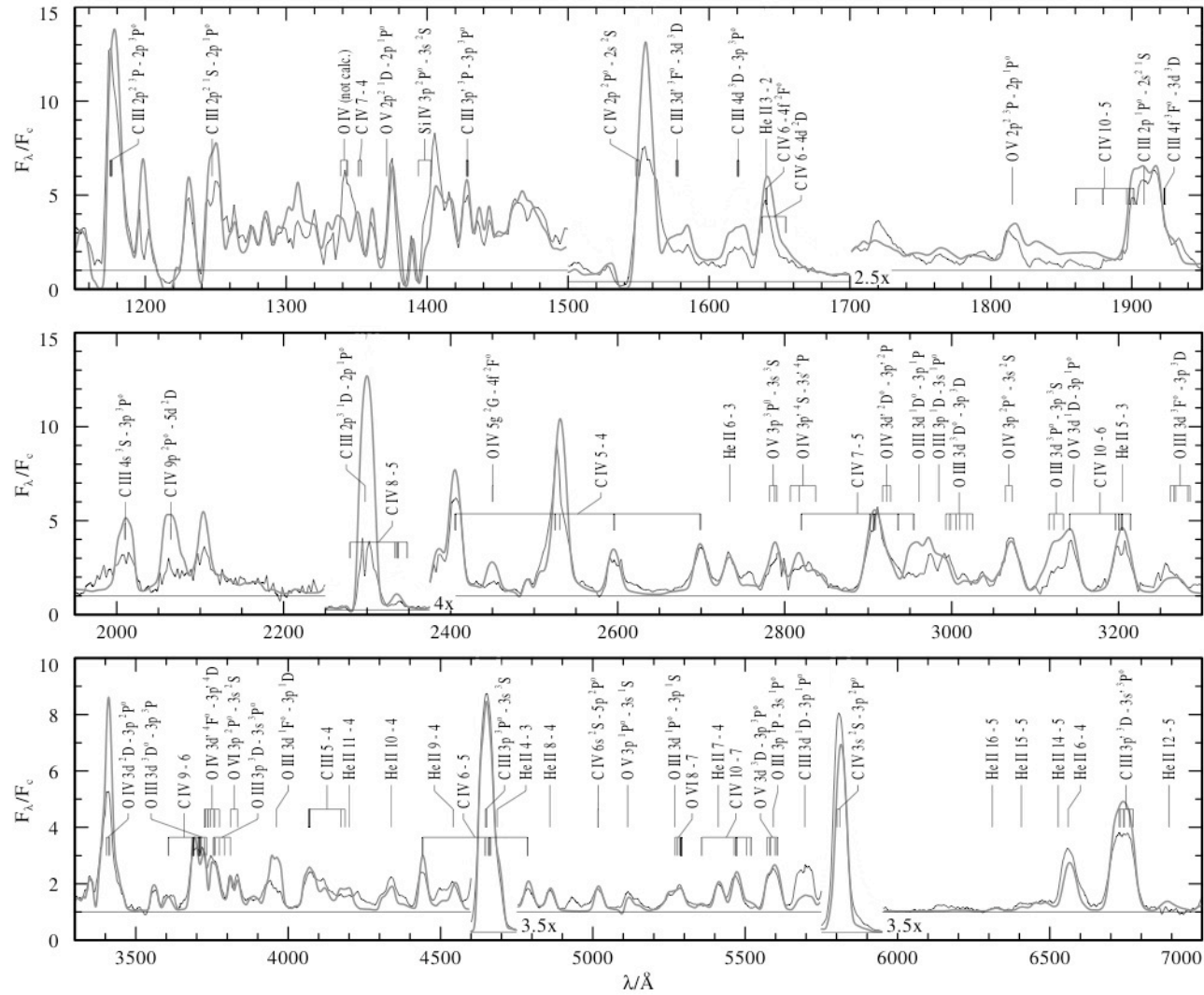
With a =sound speed we have

$$v \frac{dv}{dr} \left(1 - \frac{a^2}{v^2} \right) = -\frac{GM(1-\Gamma)}{r^2} + g(rad) + \left[\frac{2a^2}{r} - \frac{da^2}{dr} \right]$$

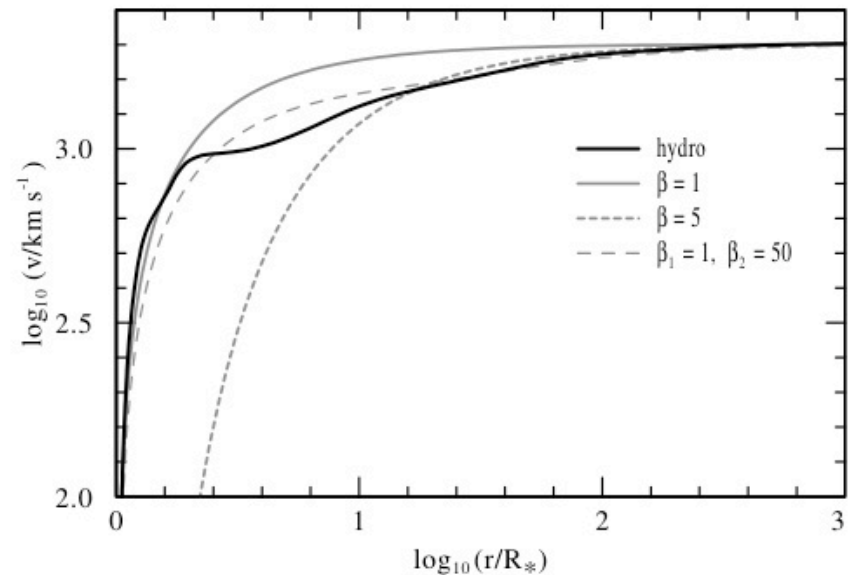
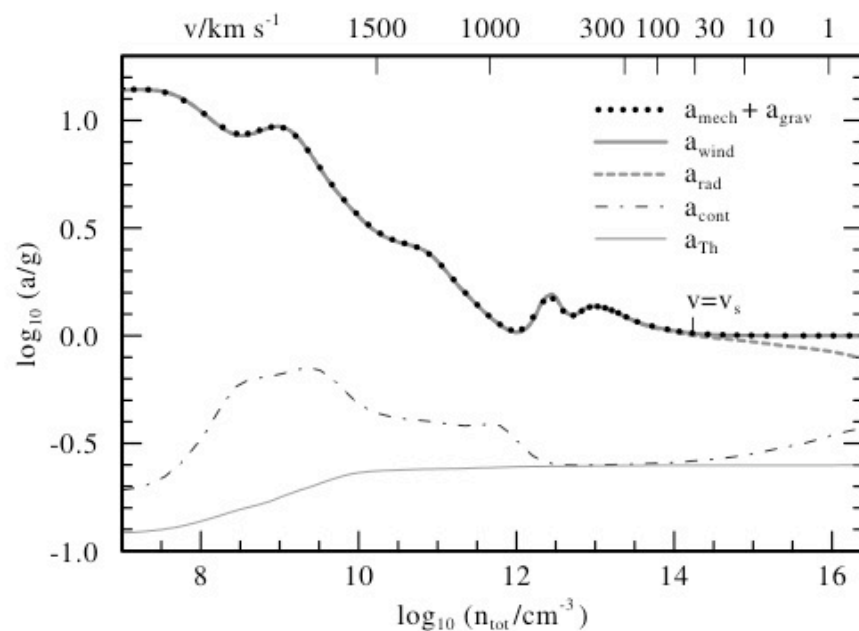
Continuum driven: The Fe bump is caused by million of lines (pseudo continuum).

$g(rad)$: only weak dependence on dv/dr

HD165763 (WR111; WC5)



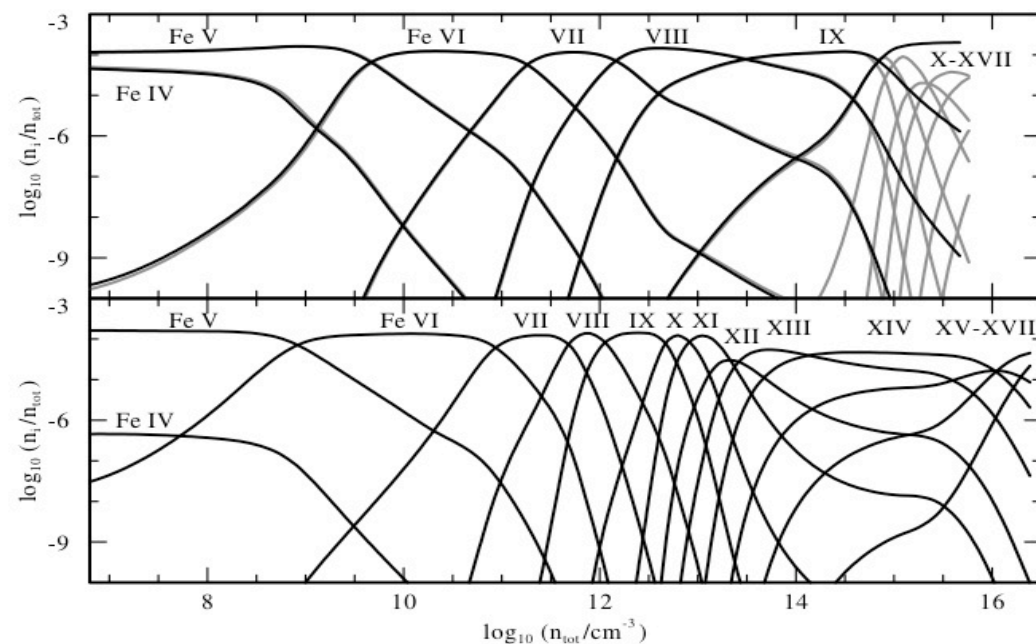
Graefener & Hamann (2005, A&A, 432, 633)



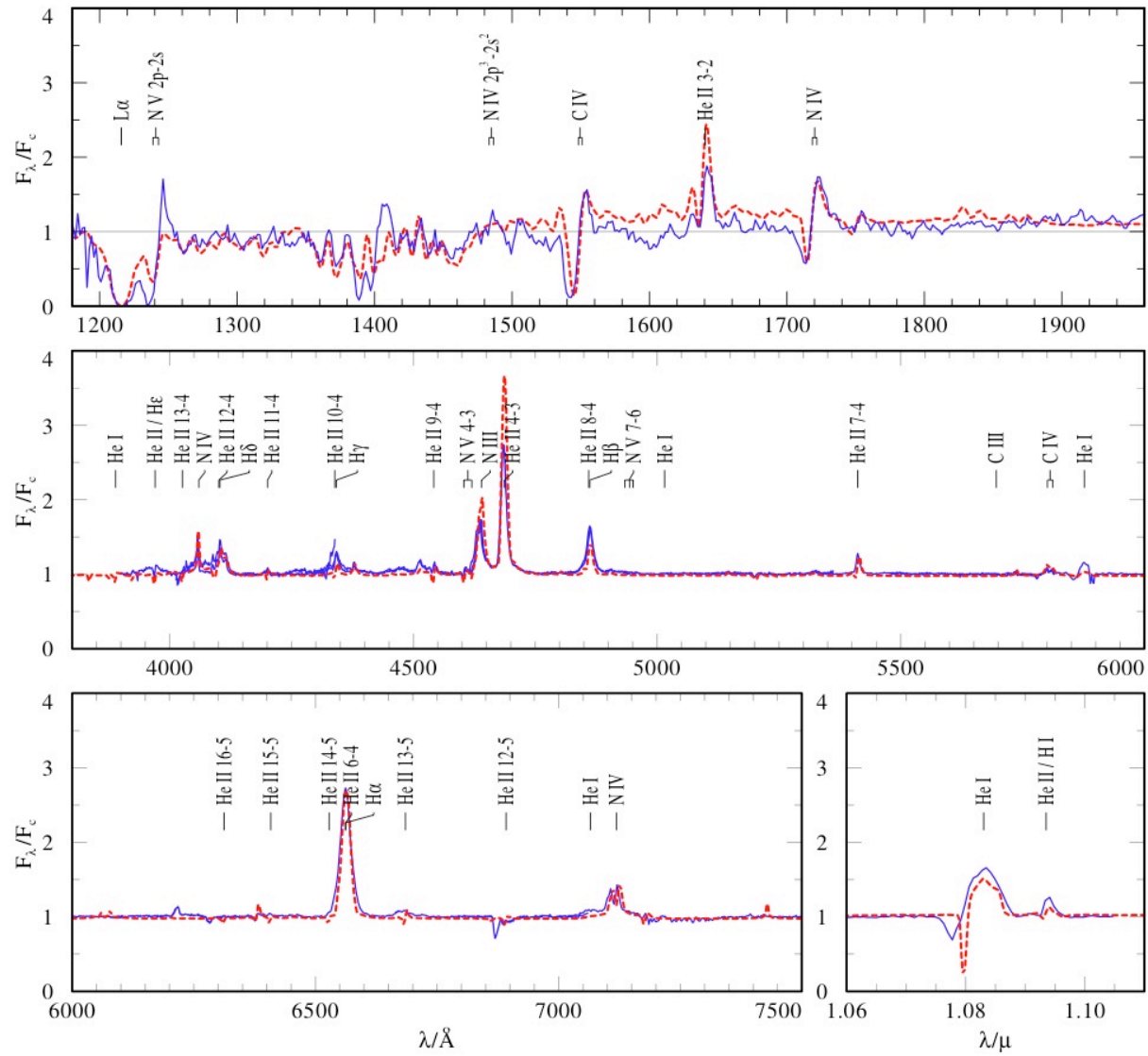
For WCE, WNE stars
necessary to include very
high ionization stages of
Fe.

Graefener & Hamann
(2005, A&A, 432, 633)

CAK alpha close to 0 (i.e.,
winds driven by thin lines.)



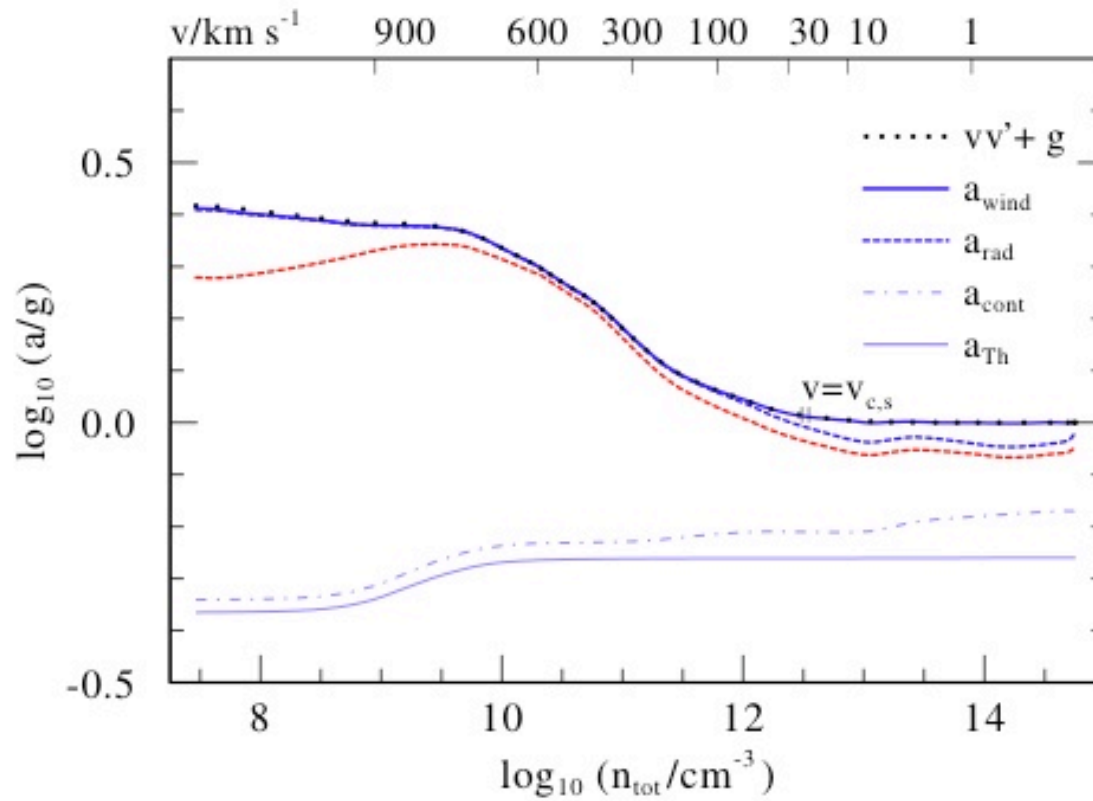
WR22 (WN7+0 system; HD 92270)



Graefener & Hamann (2008, A&A, 482, 945)

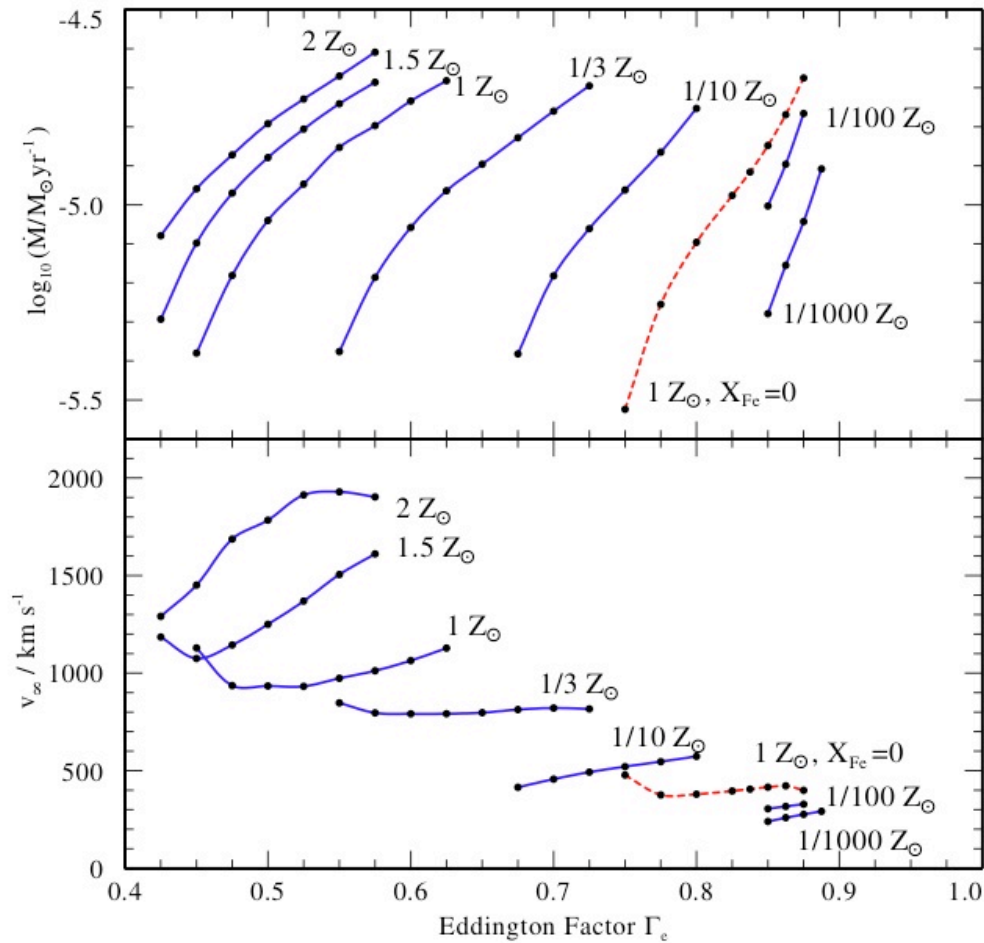
WR22: Dynamical Comparison

Blue (VD=100 km/s); Red (VD=50 km/s).



Graefener & Hamann (2008, A&A, 482, 945)

Mass loss rate is a strong function of the Eddington Parameter (Γ)



Models computed for
fixed $L(=2 \times 10^6 L_{\odot})$

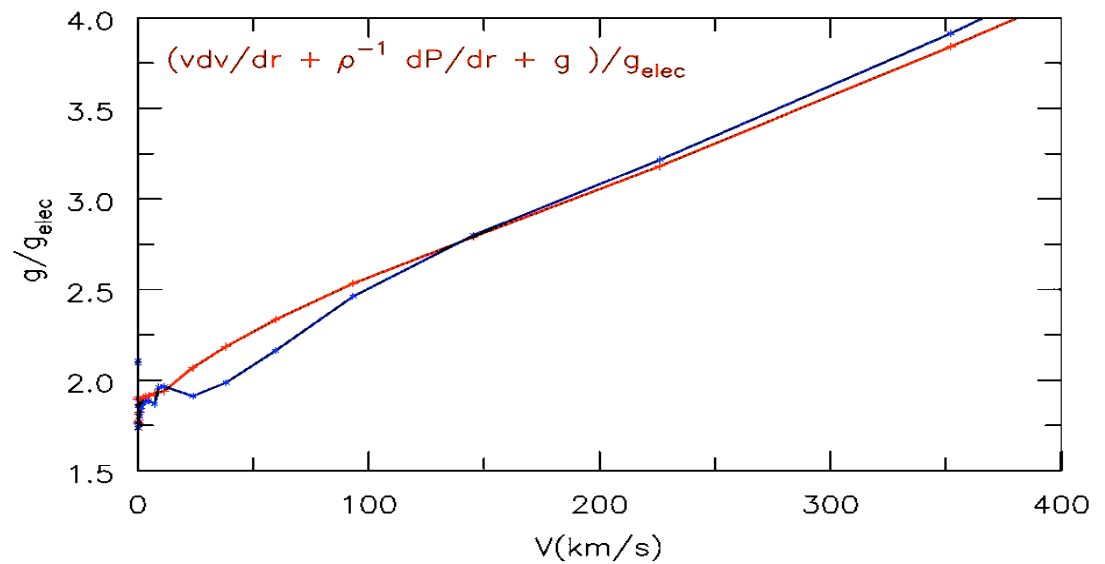
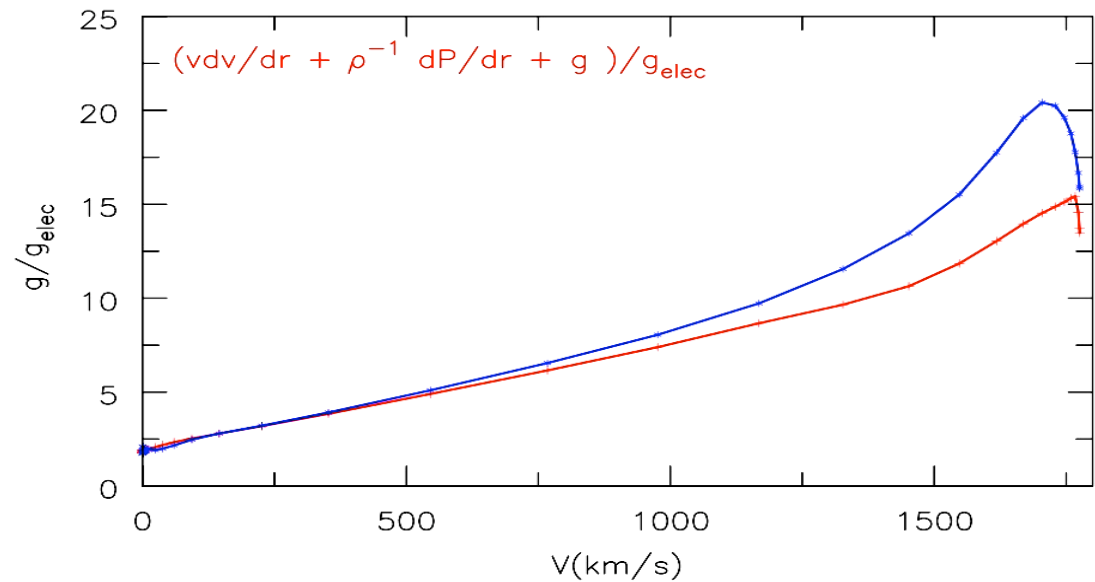
Graefener & Hamann (2008, A&A, 482, 945)

HD 92740 (WN7)

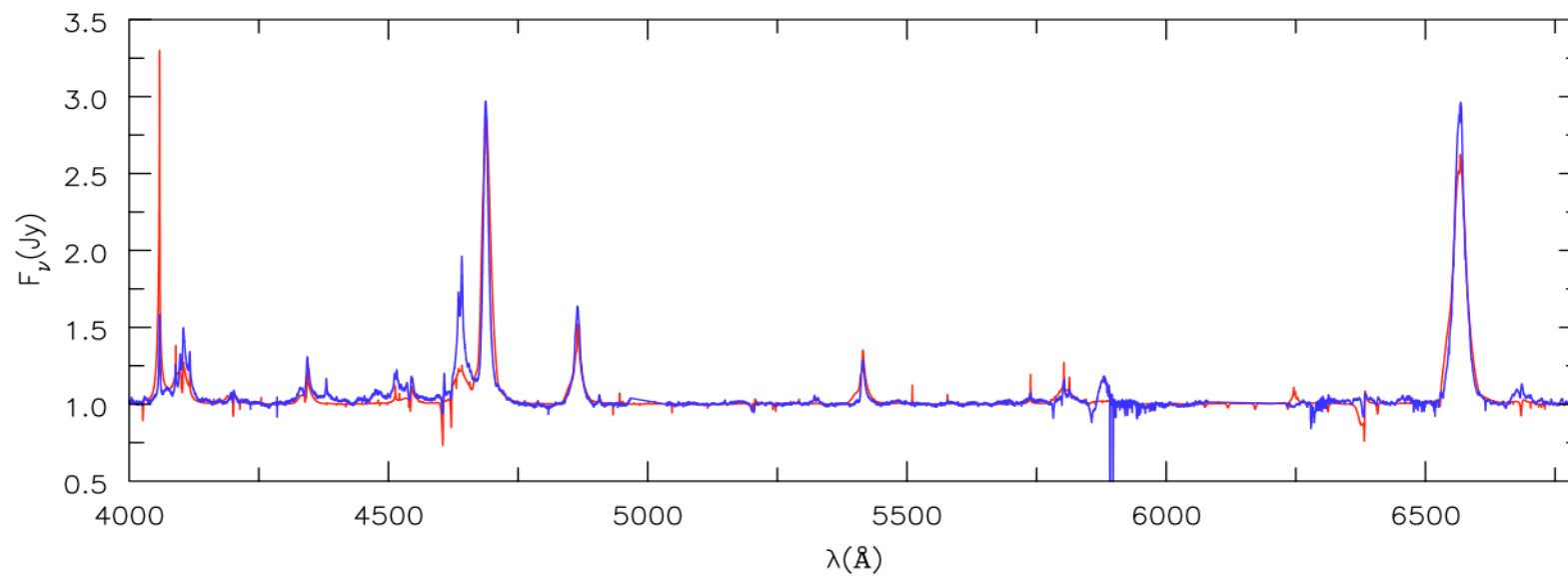
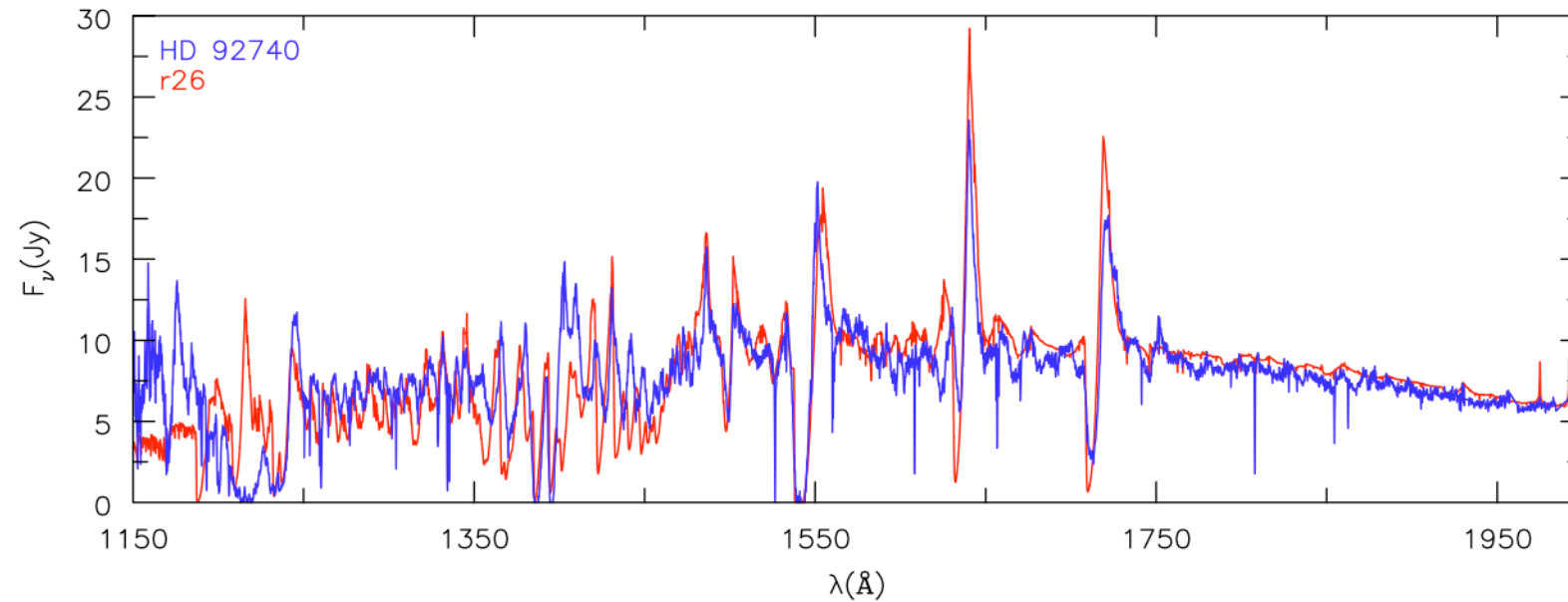
$L = 2 \times 10^6 L_{\text{sun}}$
 $\dot{M} = 2.0 \times 10^{-5} M_{\text{sun}}/\text{yr}$
 $T_{\text{eff}} = 44,000 \text{ K}$
 $\text{Mass} = 87 M_{\text{sun}}$
 $V_{\text{inf}} = 1785 \text{ km/s}$
 $V(\text{cl}) = 30 \text{ or } 100 \text{ km/s ?}$

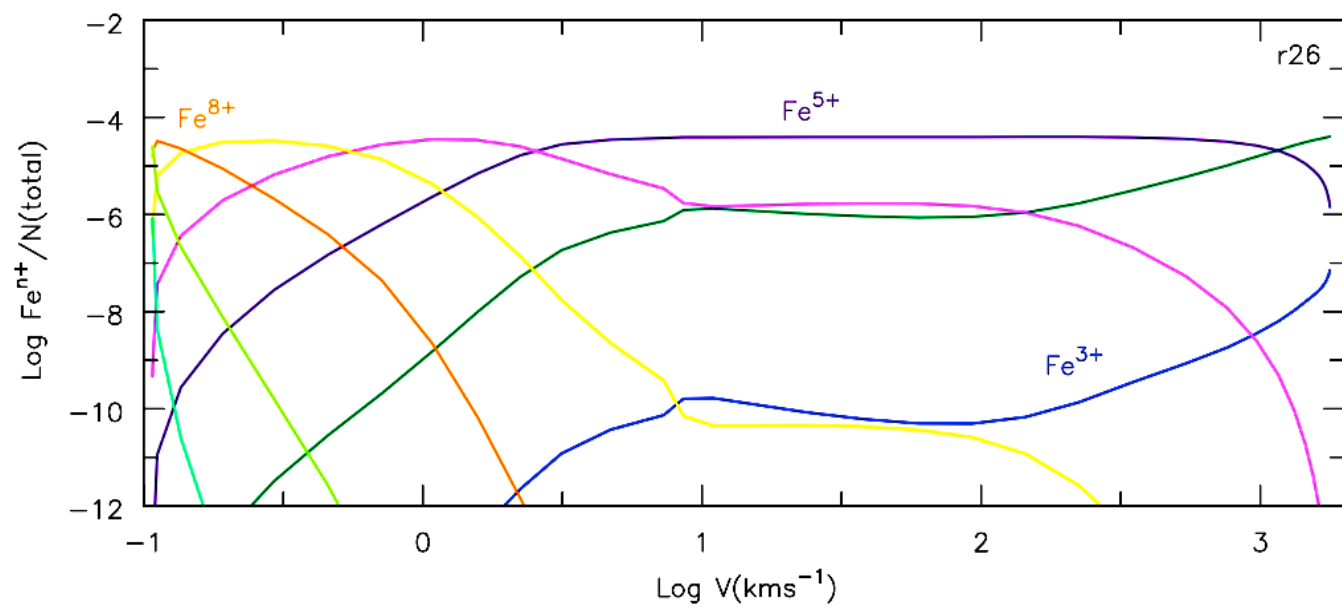
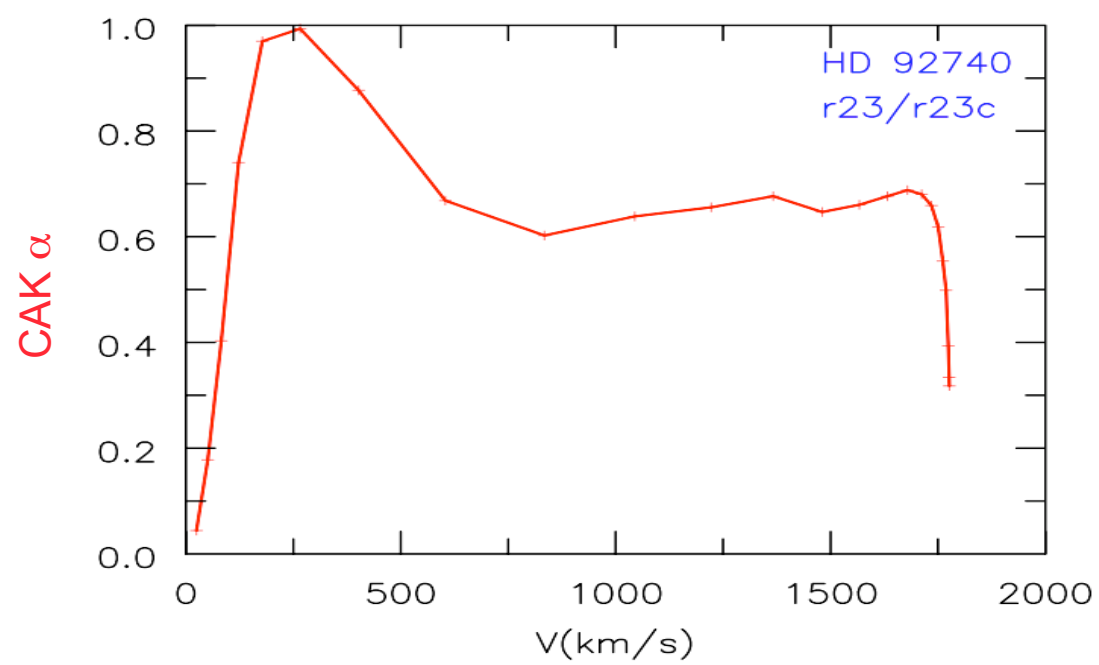
Species included

H, He, C, N, O, Ne,
 Si, S, Cl, Ar, Ca, Fe, Ni



Model with current parameters is a “little too hot”. Low ionization features (e.g., NIII 4640, HeI 5876) are too weak.





Pulsations

Strange Mode Instabilities

Occurs when radiation pressure is important.
Opacity modified acoustic waves.

Glatzel & Kiriakidis (1993, MNRAS, 263, 375)

Glatzel & Kaltssmidt (2002, MNRAS, 337, 743)

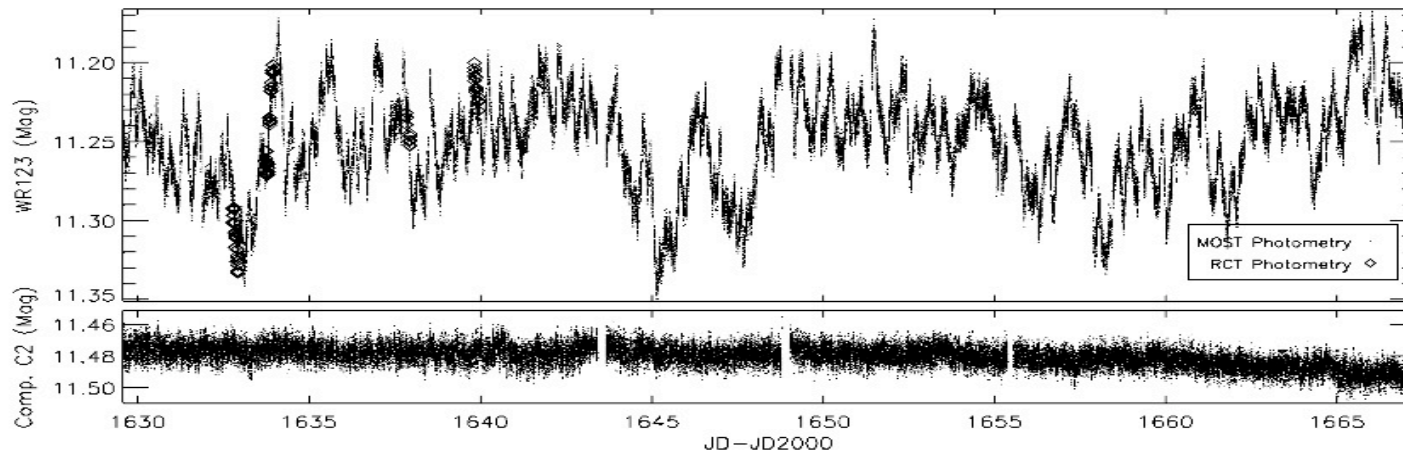
Glatzel (1994, MNRAS, 271, 61)

MOST observations: HD 165763 (WC5, WR111):

No coherent fourier amplitudes greater than 50 parts/ million for periods < 2.4 hr). Expected periods: 10 to 30 minutes.

Moffat et al. (2008, ApJ, 679, L45)

Pulsations



MOST observations of WR123 (WN8)

Lefèvre et al., Ap J, 2005, 634, L109

Stable 9.8 hour period.

$< 2 \text{ mmag}$ ($10 \text{ d}^{-1} < f < 1400 \text{ d}^{-1}$)

Complex power spectra with amplitudes 5-20 mmag.

WR103 (WC8) shows similar complex power spectra.

Dorfi , Gautschy, & Saio, 2006, A&A, 453, L35

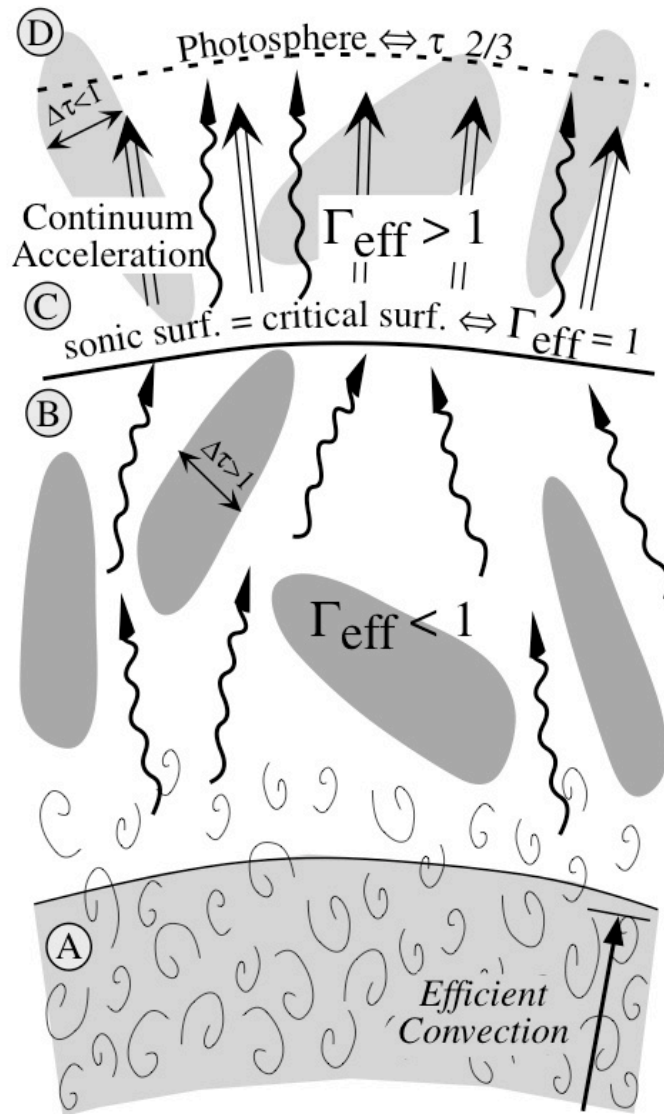
Pulsation periods consistent with 10 hours.

Pulsations damped/modified by wind

Motions outer layers not synchronized with the pulsations

Velocities of $\sim 100 \text{ km/s}$ (up & down)

Hydrodynamic Instabilities in Atmospheres Near the Eddington Limit



Instabilities

> 0.5 to 0.8

Lead to inhomogeneities

Continuum driven winds

Larger mass-loss rates.

Super Eddington Luminosities.

Eta Carinae

Novae

Modeling with Clumping

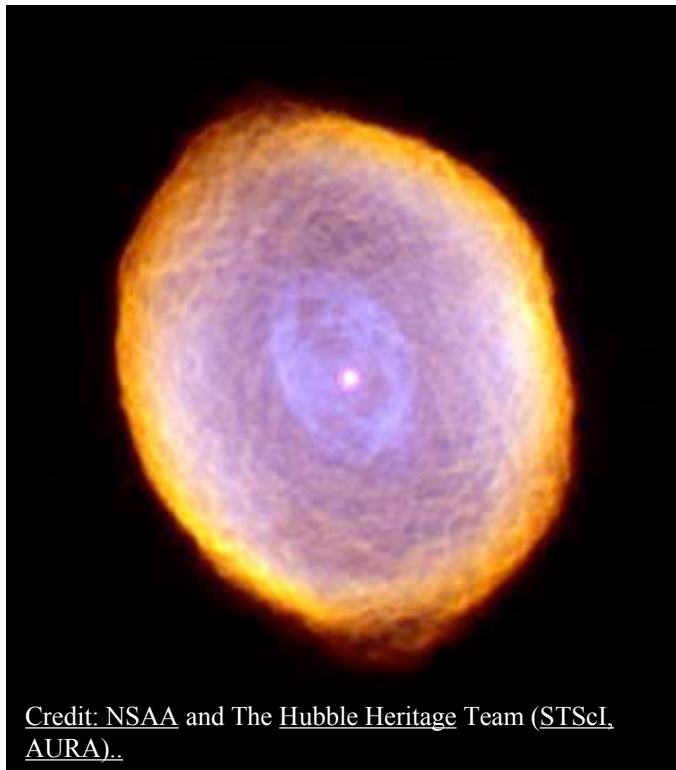
The answer you get depends on the nature of the clumps. To constrain the effects of clumping it is essential that we understand the clumping mechanism and hence the type of clumps.

Disks: Macroscopic clump.

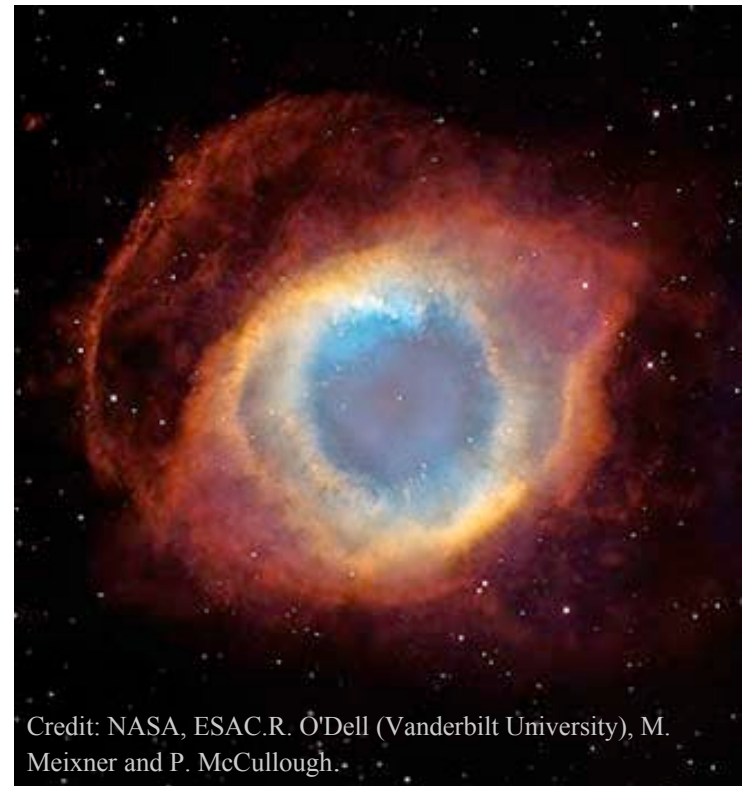
Bullets: Can have lots of mass but can't be seen spectroscopically.

Balls or pancakes --- effects, for example, porosity.

Nature of interclump medium?



Credit: NSAA and The Hubble Heritage Team (STScI, AURA).



Credit: NASA, ESAC.R. O'Dell (Vanderbilt University), M. Meixner and P. McCullough.

General Thoughts

Specification

Size & density distribution.

Velocity profile and distribution.

Nature of the interclump medium.

Amount of mechanical energy deposited, and where.

Effects

Allow lower mass-loss rates

Enhanced emission (density squared effects)

Porosity

Different lines and continua can have distinct responses, but many are (surprisingly) similar (e.g., $\propto \rho$ or ρ^2).

Potential problems (Williams 1992, ApJ, 392, 99)

Degeneracy

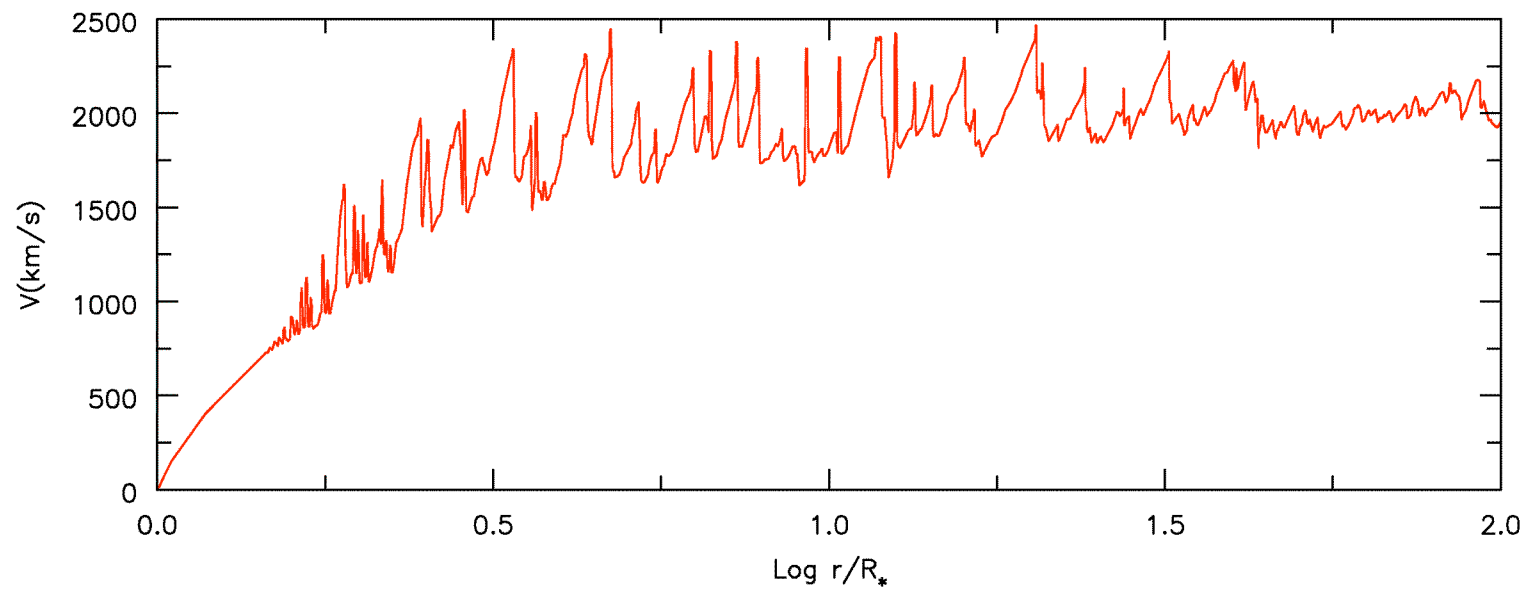
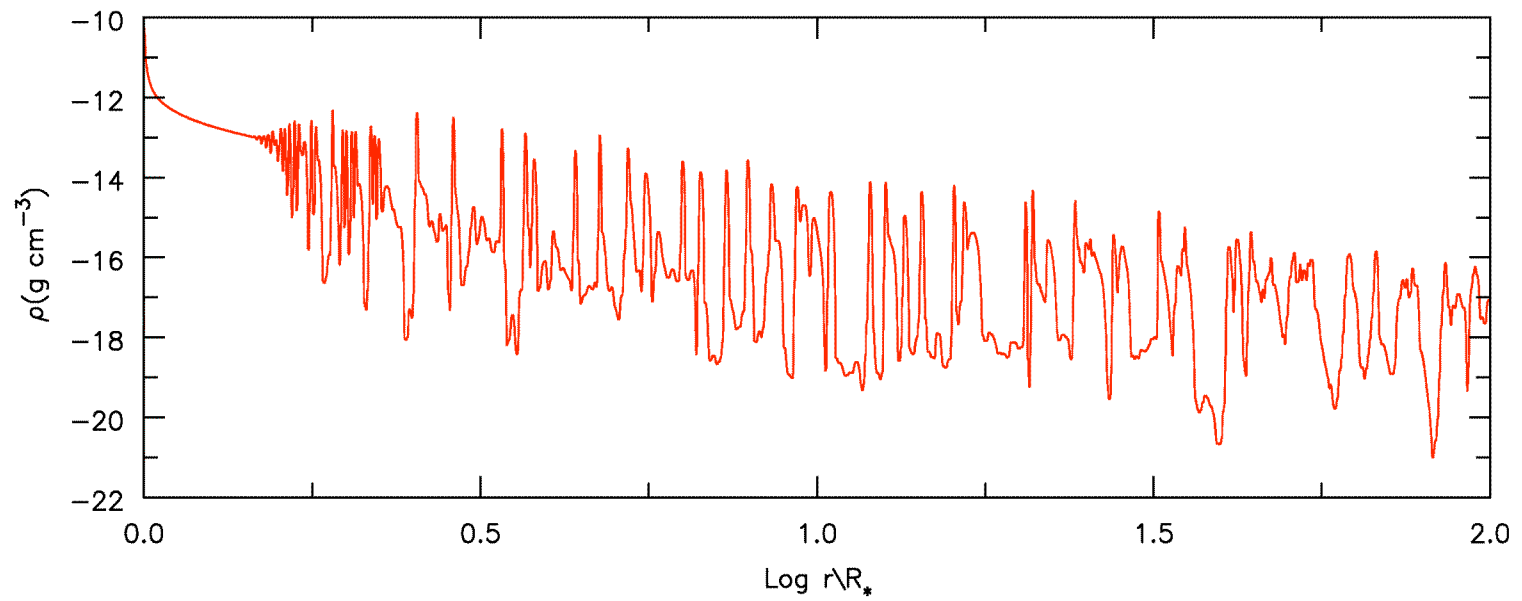
Optically thick clumps.

Clumps can have their own ionization structure.

Shielding

Non-spherical (driven: rotation, pulsations, inhomogeneities)

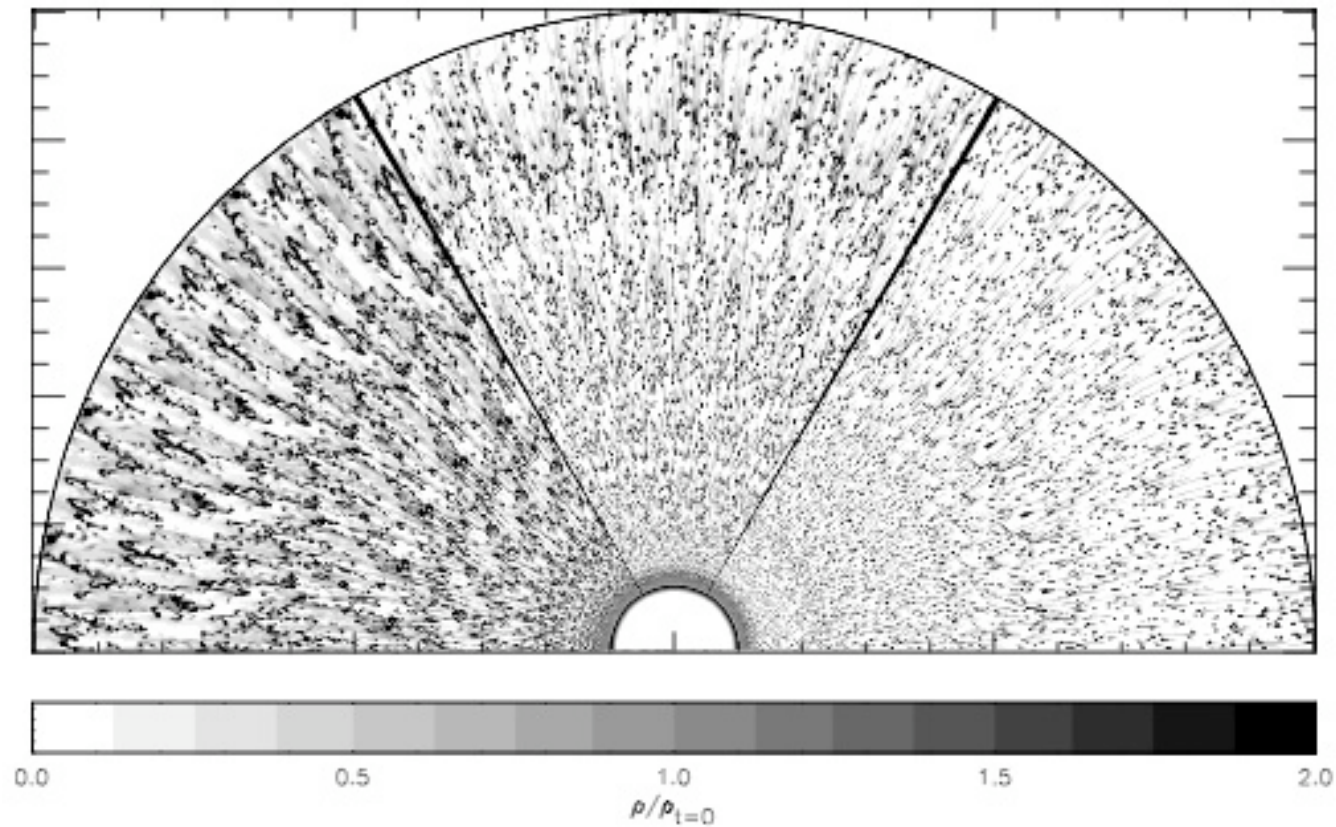
Owocki (Zeta Pup model)



e.g., Owocki, Castor, Rybicki, 1988, ApJ, 335, 914

2D Instability Simulations

Dessart & Owocki (2005, A&A, 437, 657)



Lateral Scale

Transverse Sobolev length (r/v) ~ 1 degree

Lateral scale set by grid resolution?

Diffuse radiation field crucial.

Computational Issues

Computing the spectrum (i.e., the formal solution) from a clumped model, whose populations are known, is feasible. The difficulty is computing the non-LTE populations.

Possible exception: Scattering resonance line arising from an ion which is the dominant ionization stage.

Non-LTE modeling

Homogeneous models:

$$t(2D) > 100 t(1D)$$

$$t(3D) > 5000 t(1D)$$

Inhomogeneous models:

$$t(3D) > 10^6 t(1D)$$

Can't do full problem: Need approximations.

Volume Filling Factor Approach

Assume medium is clumped, the clumps are uniform, and the fractional volume of the clumps is f . If the clumps are small compared to the photon mean-free path, then:

$$\rho(\text{clump}) = \rho(\text{smooth}) / f$$

$$\chi(\text{eff}) = f \chi(\text{clump})$$

$$\eta(\text{eff}) = f \eta(\text{clump})$$

Under these assumptions, calculation is exact.

The real world:

Approximation excellent for continua, but poor (?) for lines, since scale length of clumps is of order the Sobolev length.

Question

What is the accuracy when assumptions are not met?

How?

Many diagnostics

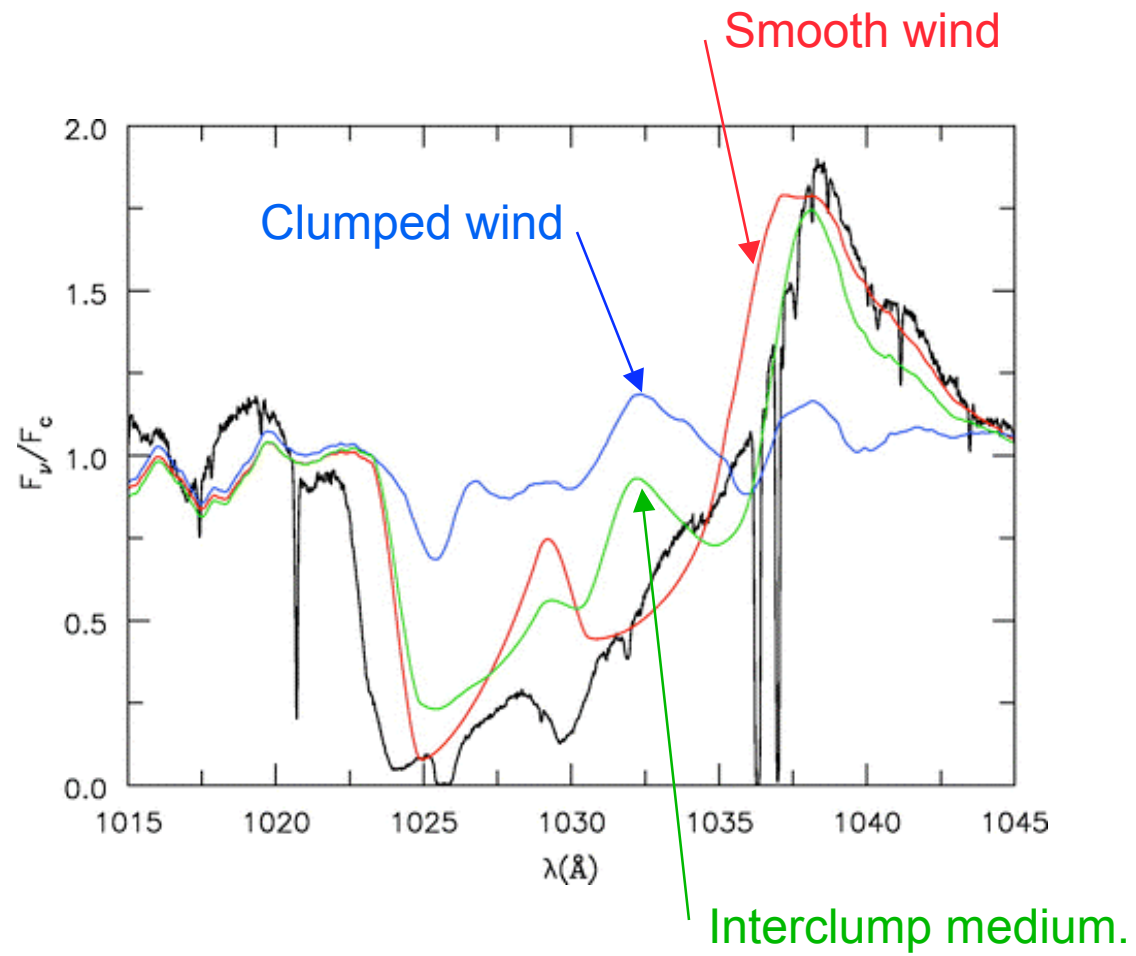
Alternative techniques

Support

Variability Observation (e.g., Lepine & Moffat, 2008)

2D simulations (e.g., Dessart & Owocki 2005)

OVI
Zeta Pup



Zsargo et al. (2008, ApJ, 685:L149)

Macro Clumping

Oskinova et al. (2007, A&A, 476, 1331)

An approximate formulation for handling optically thick clumps.

Apply model to Zeta Pup

Reasonable fit to observations

Has significant “spatial” porosity.

Is porosity important for explaining X-ray line profiles.

Mass loss rates

Lower than smooth wind results.

Higher than that obtained using volume filling factor approach.

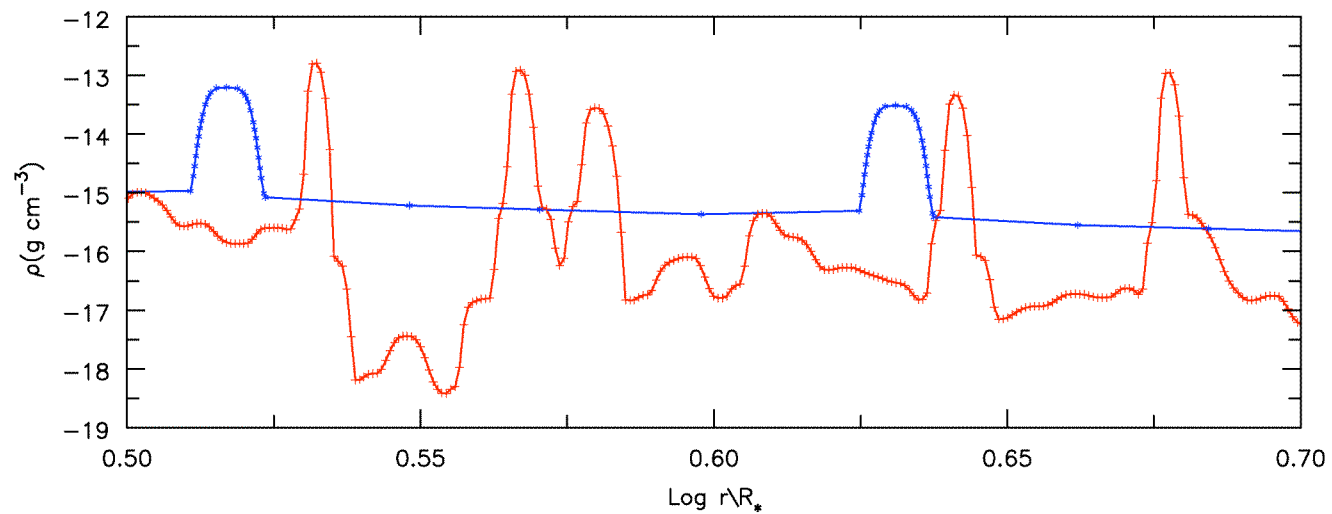
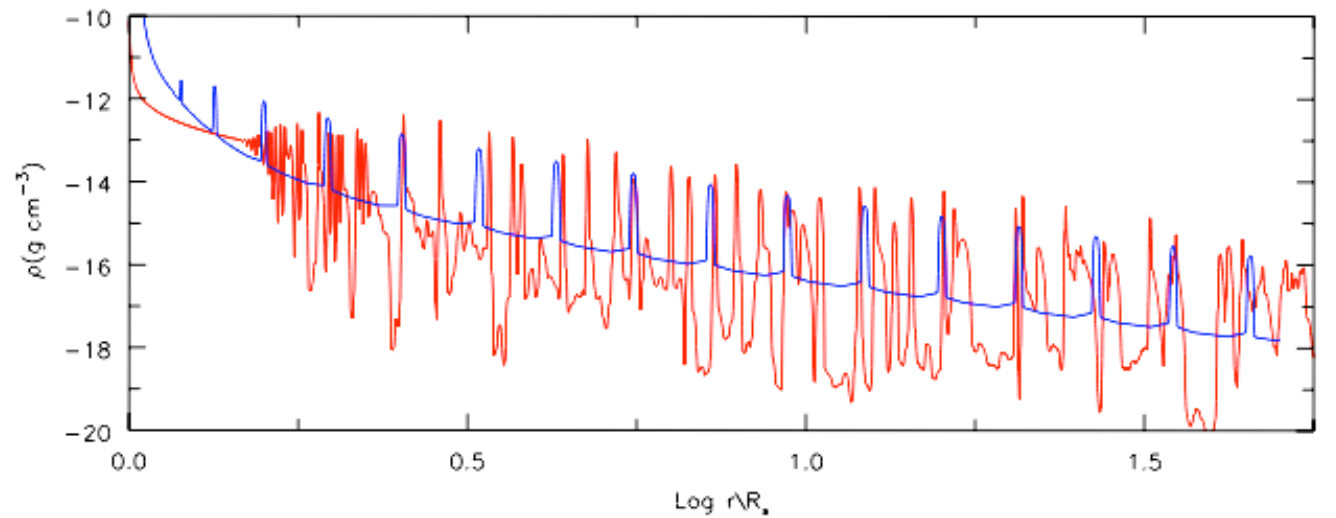
Shell model

Artificial but can be solved “exactly”

Useful for studying effects that will arise in other clumped models.

Alternative technique.

“Shell” like density structure adopted for transfer models (blue line). Red line shows radiative instability model computed for Zeta Pup by Owocki (private communication).



- ◆ For AV83 (O7 Iaf+; not shown), an shell clumping approach gives a “similar” spectrum to that obtained using the filling-factor approach, but detailed analysis required.
- ◆ For a WN5 star, the shell clump model gives a similar continuum, but generally weaker lines. The lines and continua behave differently because continuum photons generally have much greater mean free paths (hence shells are “effectively” thin) than do line photons (shells may be “effectively” thick). Since the lines are inconsistent with the continuum, clumped model is **invalid** ——— thinner clumps?

WN5 Model

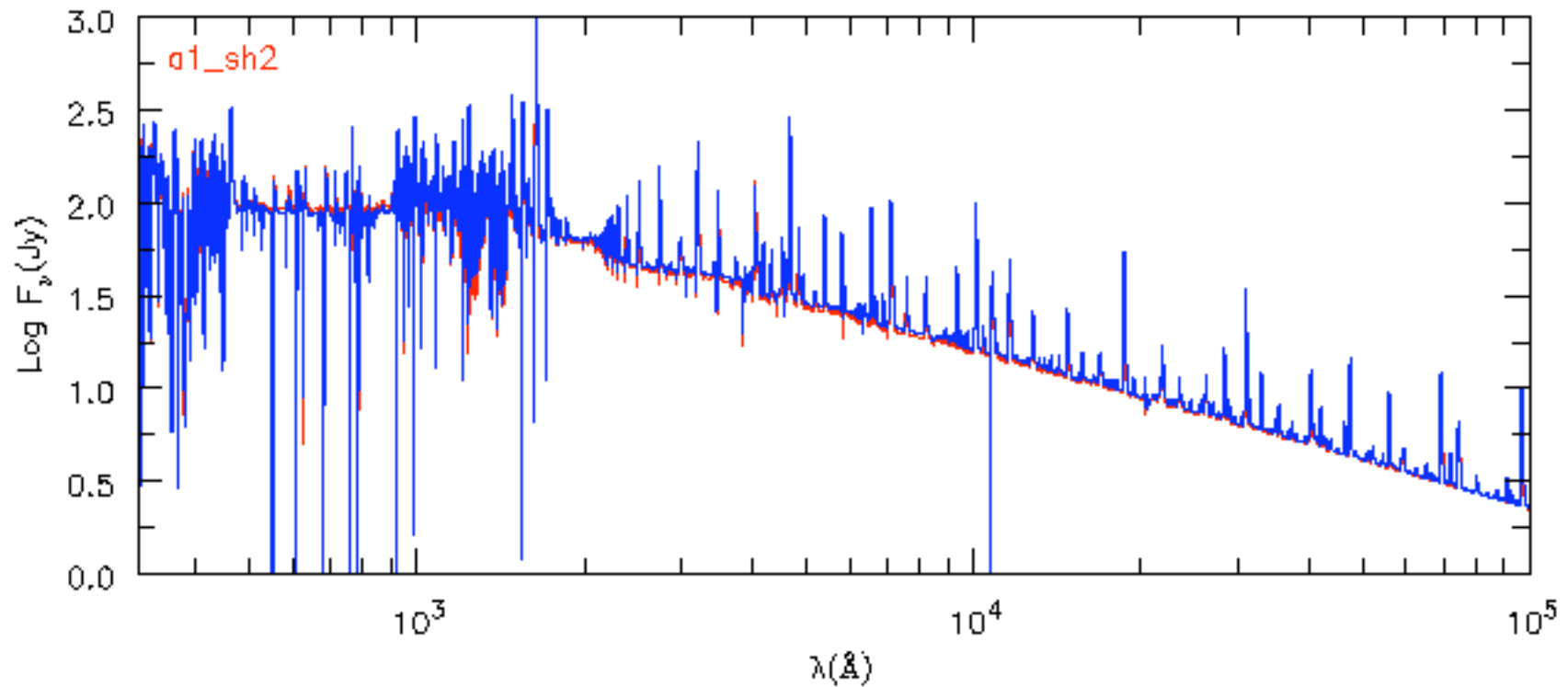
$$R_* = 2.5 R_{\odot}$$

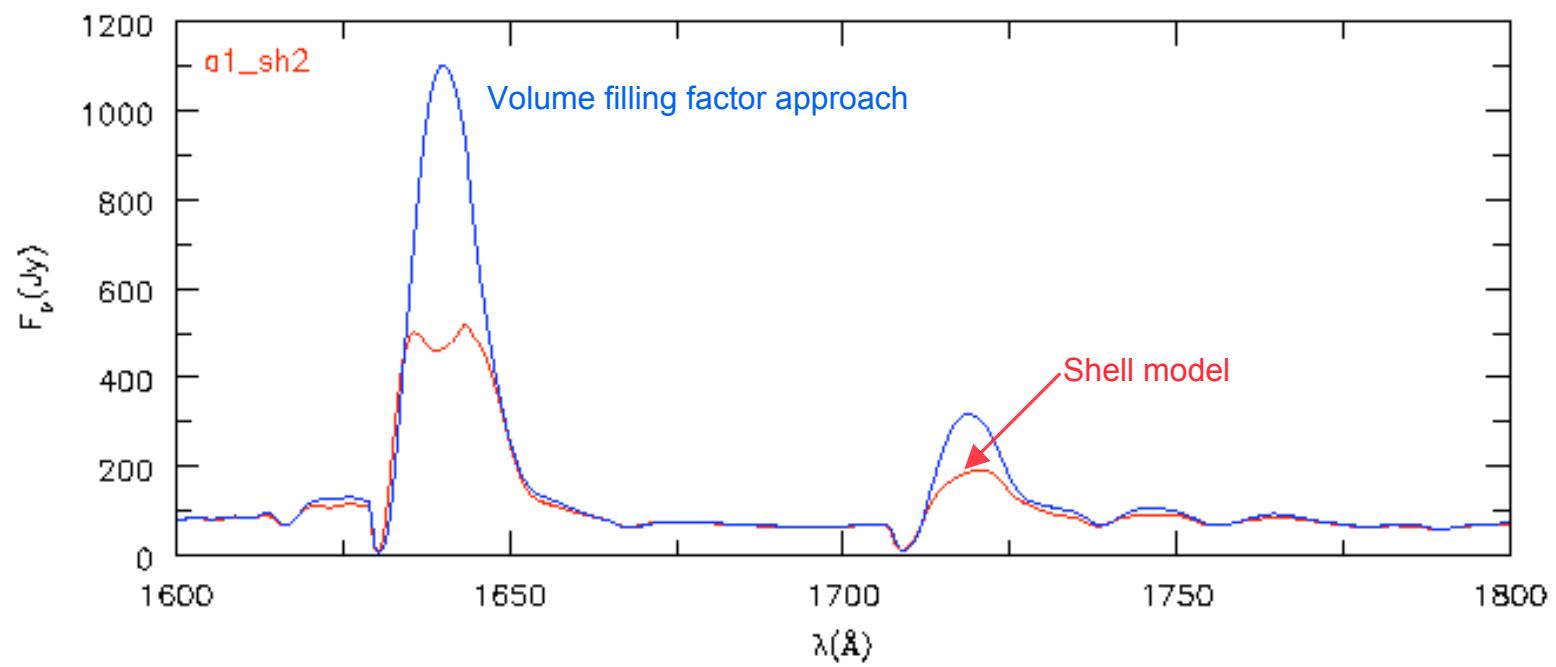
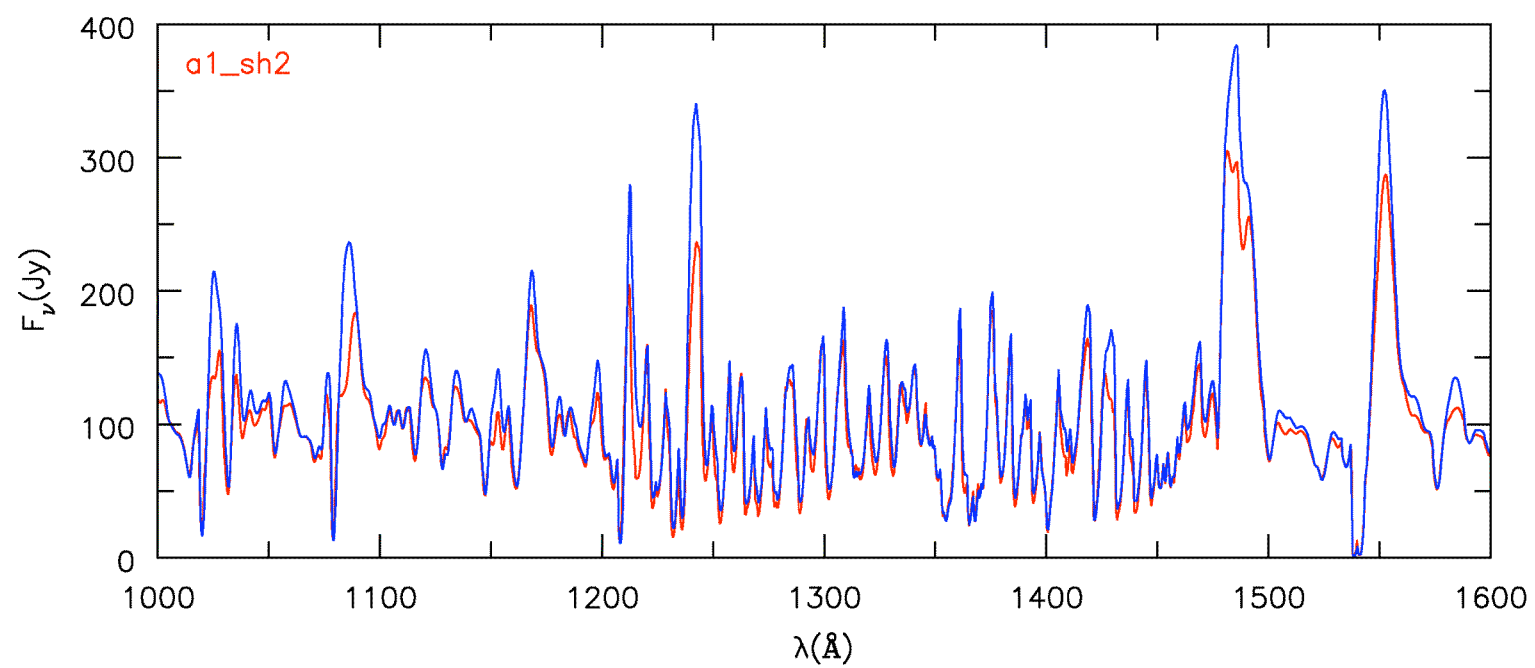
$$f = 0.1 \text{ (} V \sim 100 \text{ km/s)}$$

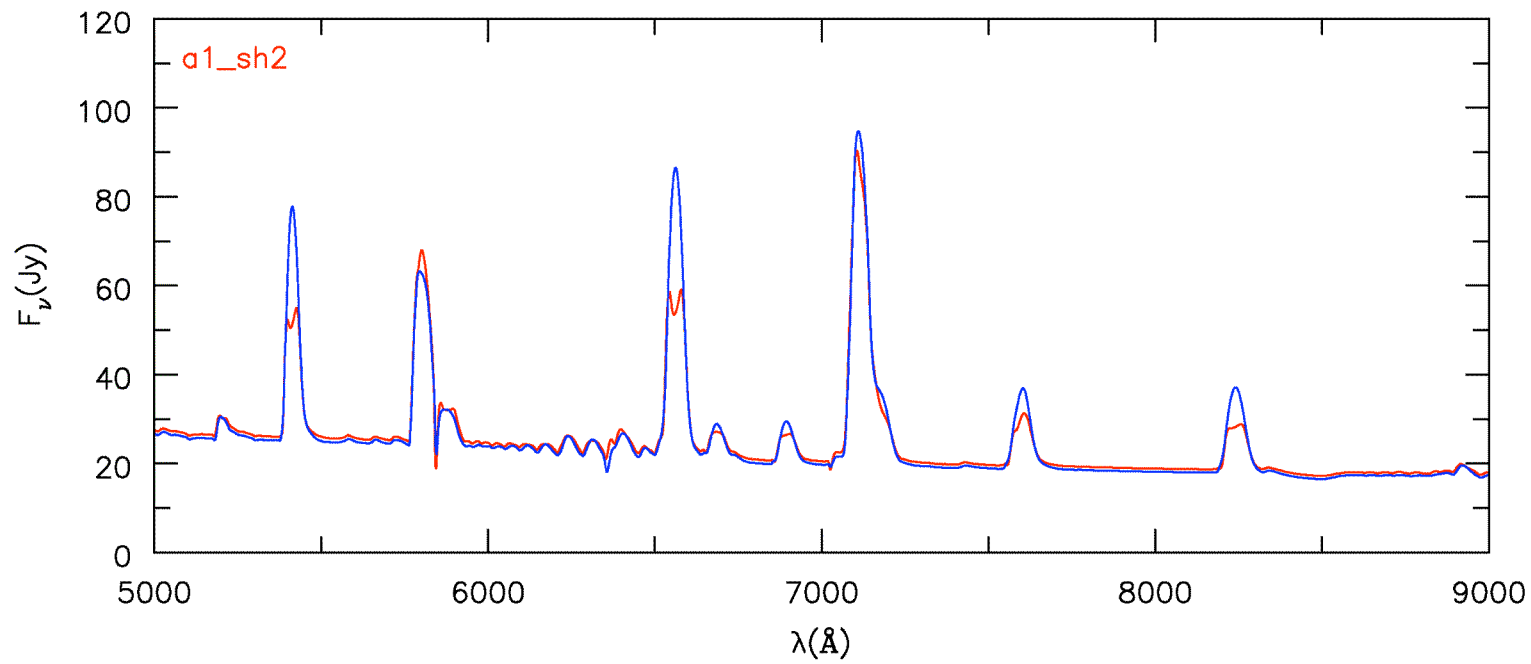
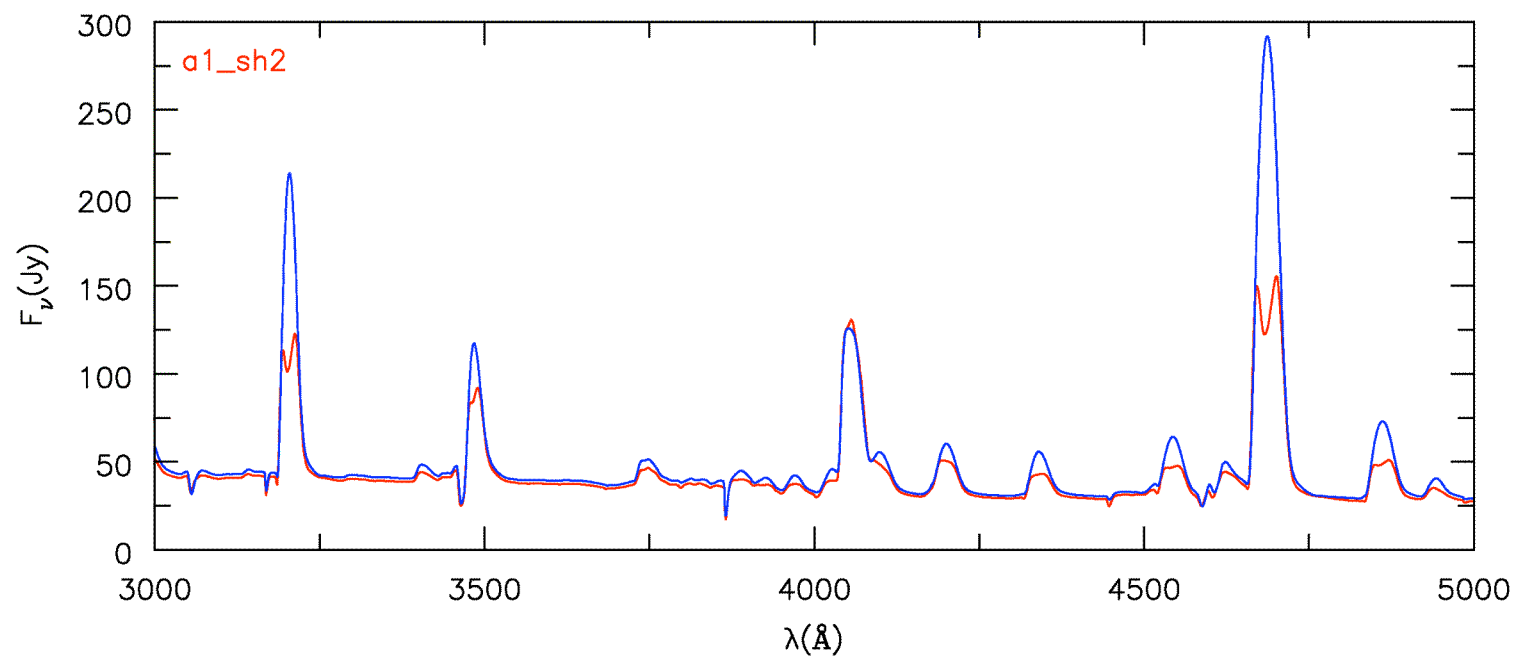
$$L = 3 \times 10^5 L_{\odot}$$

$$\dot{M} = 2.5 \times 10^{-5} M_{\odot}/\text{yr}$$

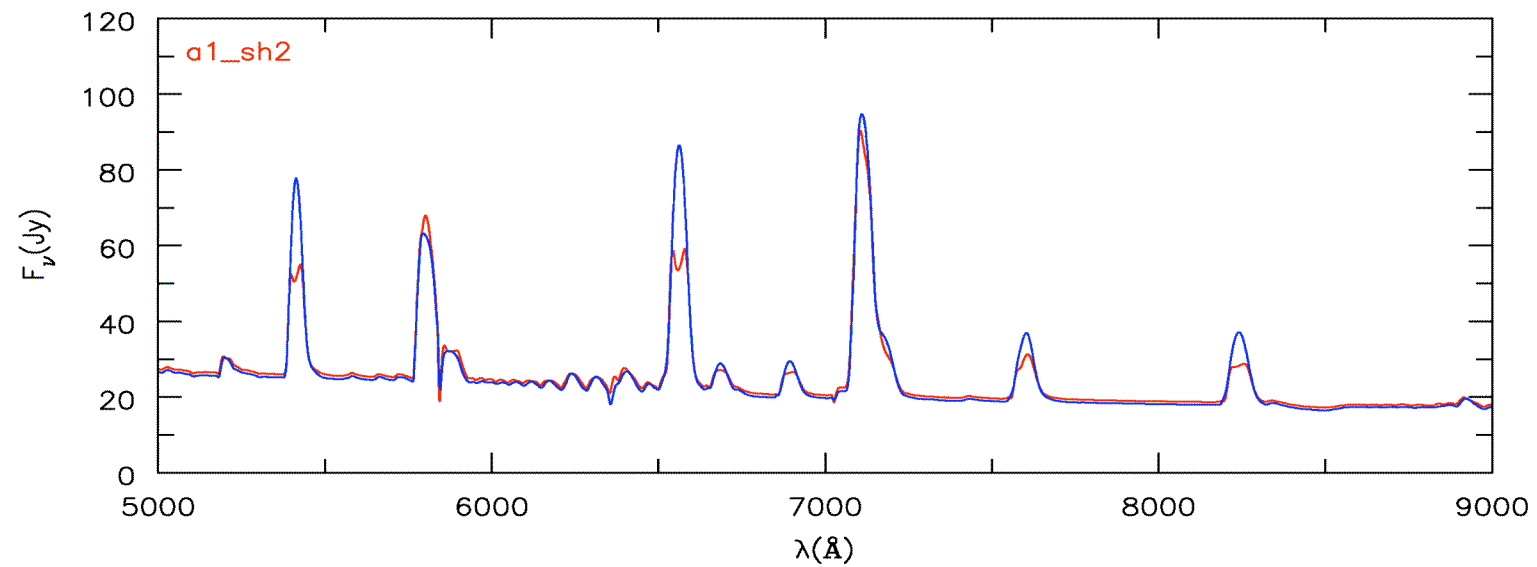
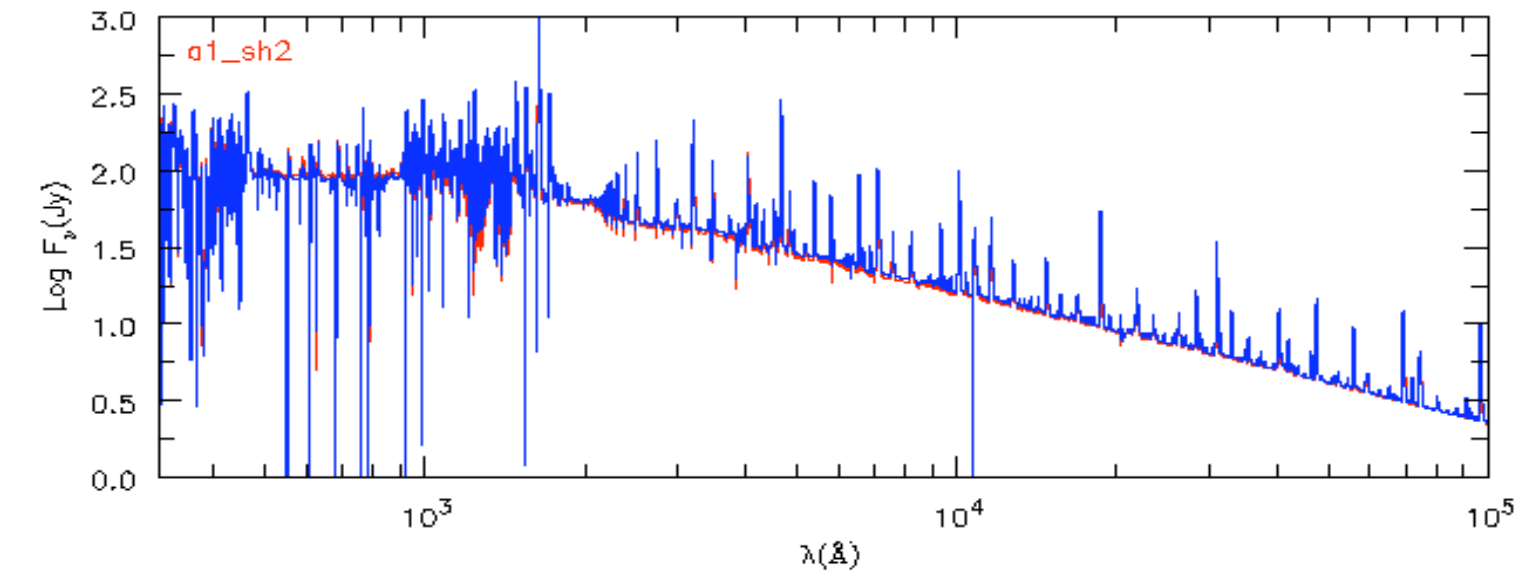
$$T_{\text{eff}} = 85,000 \text{ K}$$







Inconsistent!
Continuum matched but lines do not.



Conclusions

- ◆ The Fe opacity bumps play a key role in initiating W-R winds. Other effects (e.g., pulsations) may be needed for some W-R subclasses.
- ◆ Accuracy of current W-R models (particularly radii and effective temperatures) is limited by uncertainties in the wind hydrodynamics and clumping.
- ◆ Due to the **LARGE** number of parameters needed to parameterize clumping, need to use **ALL** available diagnostics (radio to X-ray spectra, variability) to provide constraints.
- ◆ Filling factor approach is useful, but results need verification by other means.

Urgently needed

Alternative approaches to handling clumping

Handling of complex velocity fields —→ additional diagnostics

Additional theoretical insight into clumping structure, and its variation in the wind.

Linking X-rays/structure.

THE

END